Central Limit Theorem A Demonstration of SOCR

It's Online, Therefore It Exists!

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SOCR

ATISTICS

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Outline

- What is SOCR?
- How to access SOCR
- Components of SOCR
 - Distributions
 - Experiments (CLT)
- Activities (Wiki)
- Future Research and Development

Accessing SOCR



SOCR News, Events, Announcements SOCR/CAUSEway 2007 Workshop *It's online*, *therefore it exists*! What is SOCR?

The goals of the SOCR Resource are to design, validate and freely disseminate knowledge. Our Resource specifically provides portable online aids for probability and statistics education, technology based instruction and statistical computing. SOCR tools and resources include a repository of interactive applets, computational and graphing tools, instructional and course materials.



INTERACTIVE SOCR TOOLS

SOCR Distributions SOCR Experiments SOCR Analyses SOCR Games SOCR Data Modeler SOCR Plots & Charts



FEATURES

- •60+ Experiments
- Simulations

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- Summary Stats
- •Model vs. Sample



Demonstration of CLT

Let X_1, X_2, \dots, X_n be an i.i.d. (independent and identically distributed) sample from a population that has mean μ and standard deviation σ . Then, for large n (usually n > 30) the following statement is approximately true regardless of the shape of the population:



http://www.socr.ucla.edu/

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Default Setting for SOCR CLT Applet

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A single sample of size n = 16 Normal population



A single sample of size n = 16 Exponential population

.T) Experiment	Image: Weight of the second	Stop 100								
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100 samples, each of size n = 100 Exponential population

About Snapsk	Refresh Stats Table Fit normal (1) Mean N=100 Fit normal (2) Variance N=100 0% Go To CLT Activity Histograms and Summaries Distributions									
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	Sampling Dist. of Variances, N=)))))) 0		_	Number of 100.0	Mean 18.1219	Median 18.5	SD 3.25879	Skewness 0.37446	Kurtosis -0.04444
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Future Research and Development

- SOCR usage
- Classroom testing for the effectiveness of SOCR (2005-06, 2006-07)
- New tools under development
- More SOCR activities for Wiki page
- SOCR Workshop at UCLA, August 6-8, 2007

